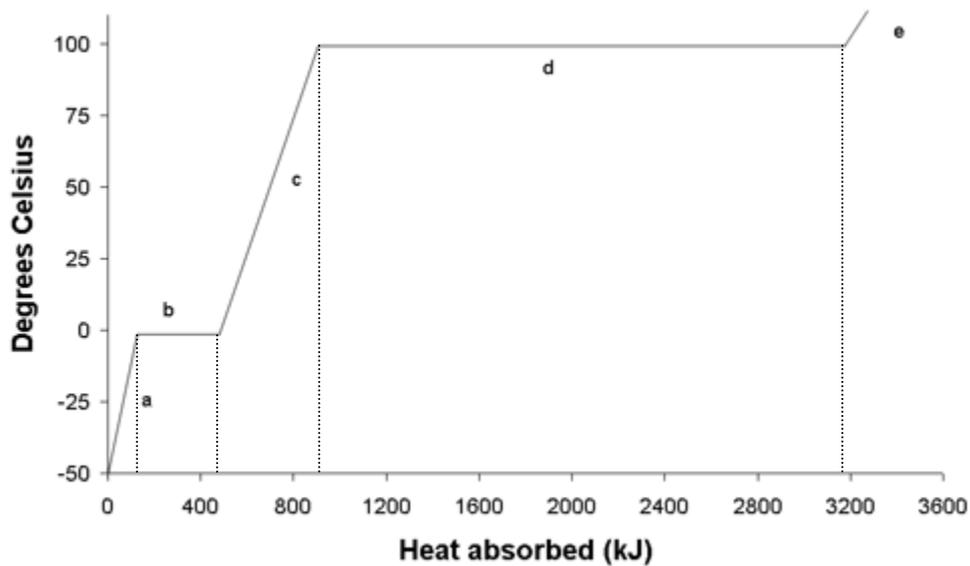


$$c_{\text{water}} = 4200 \text{ J/kgK} \quad c_{\text{ice}} = 2100 \text{ J/kgK} \quad c_{\text{copper}} = 390 \text{ J/kgK}$$

$$L_{f, \text{ice}} = 3.34 \cdot 10^5 \text{ J/kg} \quad L_{v, \text{water}} = 22.5 \cdot 10^5 \text{ J/kg}$$

Latent heat and Specific heat capacity questions.

1. How much water at 50°C is needed to just melt 2.2 kg of ice at 0°C?
2. How much water at 32°C is needed to just melt 1.5 kg of ice at -10°C?
3. How much steam at 100° is needed to just melt 5 kg of ice at -15°C?
4. A copper cup holds some cold water at 4°C. The copper cup weighs 140g while the water weighs 80g. If 100g of hot water, at 90°C is added, what will be the final temperature of the water?



5. a) Explain where the energy is going at each section of the curve from "a" to "e"
- b) Using section "b", calculate the amount of ice used to produce the graph
- c) Using section "c", calculate the amount of ice used to produce the graph

Solutions

1. How much water at 50°C is needed to just melt 2.2 kg of ice at 0°C?

Heat loss = heat gain

Heat loss of water = heat to melt ice

$$m_{\text{water}}c_{\text{water}}\Delta T = m_{\text{ice}}L_f$$

$$m_{\text{water}} * 4200 * (50 - 0) = 2.2 * 3.34 * 10^5$$

$$m_{\text{water}} = 3.50 \text{ kg}$$

2. How much water at 32°C is needed to just melt 1.5 kg of ice at -10°C?

Heat loss = heat gain

Heat loss of water = heat gain of ice + heat to melt ice

$$m_{\text{water}}c_{\text{water}}\Delta T = m_{\text{ice}}c_{\text{ice}}\Delta T + m_{\text{ice}}L_f$$

$$m_{\text{water}} * 4200 * (32 - 0) = 1.5 * 2300 * (0 - (-10)) + 1.5 * 3.34 * 10^5$$

$$m_{\text{water}} = 3.98 \text{ kg}$$

3. How much steam at 100° is needed to just melt 5 kg of ice at -15°C?

Heat loss = heat gain

Heat to condense steam + Heat loss of water = heat gain of ice + heat to melt ice

$$m_{\text{steam}}L_v + m_{\text{steam}}c_{\text{water}}\Delta T = m_{\text{ice}}c_{\text{ice}}\Delta T + m_{\text{ice}}L_f$$

$$m_{\text{steam}} * 22.5 * 10^5 + m_{\text{steam}} * 4200 * (100 - 0) = 5 * 2300 * (0 - (-15)) + 5 * 3.34 * 10^5$$

$$2.67 * 10^6 * m_{\text{steam}} = 1.84 * 10^6$$

$$m_{\text{steam}} = 0.69 \text{ kg}$$

4. A copper cup holds some cold water at 4°C. The copper cup weighs 140g while the water weighs 80g. If 100g of hot water, at 90°C is added, what will be the final temperature of the water?

Heat loss = heat gain

heat gain of cup + heat gain of cold water = heat loss of hot water

$$m_{\text{cup}}c_{\text{cup}}\Delta T + m_{\text{cw}}c_{\text{w}}\Delta T = m_{\text{hw}}c_{\text{w}}\Delta T$$

$$0.14 * 390 * (T_F - 4) + 0.08 * 4200 * (T_F - 4) = 0.1 * 4200 * (90 - T_F)$$

$$390.6T_F - 1562.4 = 37800 - 420T_F$$

$$810.6T_F = 39362.4$$

$$T_F = 48.6^\circ\text{C}$$

5. a) Explain what is occurring at each section of the curve from "a" to "e"

a - ice particles are increasing in kinetic energy, raising temperature

b- ice particles are breaking apart and increasing in potential energy as ice melts

c- water particles are increasing in kinetic energy, raising temperature

d- water particles are breaking apart and increasing in potential energy as water vaporises

e- steam particles are increasing in kinetic energy, raising temperature

b) Using section "b", calculate the amount of ice used to produce the graph

$$\Delta Q = mL_f$$

$$480 - 140 = m * 3.34 * 10^5$$

$$m = 0.001 \text{ kg (approx 1 g, with error from reading graph)}$$

c) Using section "c", calculate the amount of ice used to produce the graph

$$\Delta Q = mc\Delta T$$

$$920 - 480 = m * 4200 * (100 - 0)$$

$$m = 0.001 \text{ kg (approx 1 g, with error from reading graph)}$$